Morphology in the Age of Pre-trained Language Models

Judit Ács

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- so I shifted towards modeling and evaluation
- 1. Part I. deals with deep learning for morphology (2018-2020)
- 2. Part II. is about evaluating language models with special focus on morphosyntax (2019-2024)

Outline

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languages

Perturbations and Shapley values Shapley values

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

References

Part I. Deep Learning for Morphology

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

References

Encoder-decoder models for morphology

Encoder-decoder models for morphology Thesis 1

Encoder-decoder (a.k.a. sequence-to-sequence or seq2seq) models are well-suited for morphological inflection and generation. This holds for type-level and sentence-level tasks in multiple languages.

These contributions were published in Ács (2018).

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

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Morphological inflection



| release | V;V.PTCP;PRS | releasing |
|-------------|--------------|--------------|
| deodourize | V;NFIN | deodourize |
| outdance | V;V.PTCP;PRS | outdancing |
| misrepute | V;NFIN | misrepute |
| vanquish | V;PST | vanquished |
| resterilize | V;3;SG;PRS | resterilizes |

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

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Overview

- yearly competition computational morphology
- 2 tasks in 2018:
 - 1. Task 1: Type-level inflection
 - 110 languages
 - high (10,000), medium (1,000), low (100) data sizes
 - source: Wiktionary inflection tables
 - UniMorph schema (Kirov et al., 2018)
 - 2. Task 2: Inflection in context
 - 7 languages
- I participated as an individual team
- 3rd place in Task 1, 2nd place in Task 2

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Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

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My model for Task 1: Type-level inflection



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Neural pattern matching

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Task 1 results



Our team in orange (bme).

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Task 2: Inflection in context

| Les | le | DET;DEF;FEM;PL |
|------------|-----------|----------------|
| compagnies | compagnie | N;FEM;PL |
| aériennes | aérien | ADJ;FEM;PL |
| à | à | ADP |
| bas | bas | ADJ;MASC;SG |
| coût | coût | N;MASC;SG |
| ne | ne | ADV;NEG |
| | connaître | _ |
| pas | pas | ADV;NEG |
| la | le | DET;DEF;FEM;SG |
| crise | crise | N;FEM;SG |

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

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Uralic languages

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References

Track 2: no lemmas or tags

Inflection in context model



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Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Task 2 results



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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values Shapley values

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

References

Neural pattern matching

Differentiable neural pattern matching for morphology Thesis 2

Differentiable neural pattern matching can extract morphosyntactic patterns in multiple languages when used as an encoder for morphological inflection and analysis.

Ács and Kornai (2020) was awarded the best paper award at the Hungarian Computational Linguistics Conference in 2020.

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

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Overview

- Schwartz et al. (2018) introduced SoPa or Soft Patterns, a differentiable pattern learner
- restricted to fixed length linear patterns with epsilon transitions and self-loops
- fully differentiable and end-to-end trainable
- they used it for sequence classification in English, token based



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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

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Perturbations and Shapley values Shapley values

My additions

- I reimplemented it as an encoder of an encoder-decoder model
- the decoder is an LSTM initialized with the final state of the SoPa encoder
- applied it at the character level
- each pattern matches a character span or subword

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languag

Perturbations and Shapley values Shapley values

Task

analysis

analysis

analysis

analysis

copy

copy

copy

copy

lemmatization

lemmatization

lemmatization

lemmatization

Language Hungarian

Hungarian

Hungarian

Hungarian

Hungarian

Hungarian

English

French

English

French

English

French

Source

vásároljanak

désinstalleriez

vásároljanak

désinstalleriez

vásároljanak

désinstalleriez

lepkékben

hugging

lepkékben

hugging

lepkékben

hugging

Target

vásárol

lepke

hug

N IN+ESS PL

V V.PTCP PRS

V COND 2 PL

désinstaller

vásároljanak

désinstalleriez

lepkékben

hugging

V SBIV PRS INDF 3 PL

| Morphology in the |
|--------------------|
| Age of Pre-trained |
| Language Models |

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Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

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| The source i | is the | same | in all | three | tasks. |
|--------------|--------|------|--------|-------|--------|
|--------------|--------|------|--------|-------|--------|

Experimental setup

- 120 patterns: 40 3-long, 40 4-long, 40 5-long
- 12 typologically diverse languages
- 10,000 train, 2,000 dev, 2,000 test word types
- baseline: both the encoder and the decoder are LSTMs with attention
- SoPa seq2seq: SoPa encoder, LSTM decoder with attention on intermediate SoPa outputs

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

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Neural pattern matching Results



- the baseline is always better
- SoPa is not good at copying and lemmatization
- noticably better at morphological analysis

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values Shapley values

Model similarity

- We define a similarity metric between two SoPa seq2seq models (M₁ and M₂) that work on the same input
- take the highest scoring T patterns for each input and compare the subwords
- for each pattern by M₁, find the most similar pattern in M₂
- average it over a dataset

Sim
$$(M_1, M_2, D) = \frac{1}{|D|} \sum_{d \in D} S(M_1(d), M_2(d))$$

$$S(M_1(d), M_2(d)) = \frac{1}{2T} (\sum_{p_i \in P_1} \max_{p_j \in P_2} J(p_i, p_j) + \sum_{p_j \in P_2} \max_{p_i \in P_1} J(p_i, p_j))$$

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Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic langua

Perturbations and Shapley values Shapley values

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

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Uralic language

Perturbations and Shapley values Shapley values

References

Neural pattern matching

Model similarity example

| | ^ablakban\$ | ^abl <mark>akb</mark> an\$ | ^ablak <mark>ban</mark> Ş | ^ablak <mark>kban</mark> \$ | Мах |
|----------------------------|-------------|----------------------------|---------------------------|-----------------------------|-------|
| ^ablak <mark>ban</mark> \$ | 0 | 0.2 | 1 | 0.75 | 1 |
| ^abla <mark>kba</mark> n\$ | 0 | 0.5 | 0.5 | 0.75 | 0.75 |
| ^ab <mark>lak</mark> ban\$ | 0 | 0.5 | 0 | 0.167 | 0.5 |
| ^ab <mark>lakb</mark> an\$ | 0 | 0.75 | 0.167 | 0.33 | 0.75 |
| Max | 0 | 0.75 | 1 | 0.75 | 0.685 |

Similarity results



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Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values Shapley values

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

References

Part II. Evaluating Pre-trained Language Models

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values Shapley values

References

Morphosyntactic probing of PLMs

Morphosyntactic probing of PLMs Thesis 3

Pre-trained language models (PLMs) trained on unannotated text learn morphology. PLMs' representations retain morphosyntactic information across a large set of typologically diverse languages and multiple tasks. This information can be recovered via probing or diagnostic classifiers.

These contributions were published in (Ács, 2019; Ács et al., 2021; Acs et al., 2023).

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Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

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Perturbations and Shapley values Shapley values

Morphosyntactic probing of PLMs

Background

- Pre-trained Language Models or PLMs are probabilistic models of natural (written) language
- pre-trained on large unannotated text
- we mainly deal with masked language models
- contextual models
 - sentence representation (or longer)
 - word representation depends on the context
- BERT model family
- English and multilingual, later many language and domain specific
- evaluation by probing
 - take a set of annotated text
 - train a small classifier on top of the PLM's representation
 - if it performs well, the information is available in the model

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Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

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Perturbations and Shapley values Shapley values

Probing architecture



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Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

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Uralic languages

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Universal Dependencies

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ntactic/ PLMs

| Form | UPOS | Morphological features | |
|------------|-------|--|------------------------|
| The | DET | Definite=Def PronType=Art | |
| third | ADJ | Degree=Pos NumType=Ord | |
| was | AUX | Number=Sing Person=3 Tense=Past VerbForm=Fin | Morphosy probing of |
| being | AUX | VerbForm=Ger | Subword pool |
| run | VERB | Tense=Past VerbForm=Part Voice=Pass | Morphology i |
| by | ADP | | |
| the | DET | | |
| head | NOUN | Number=Sing | Hungarian |
| of | ADP | | Uralic languaş |
| an | DET | _ Definite=Ind PronType=Art | |
| investment | NOUN | Number=Sing | Shapley value |
| firm | NOUN | Number=Sing | Reference |
| | PUNCT | _ | |
| | | | |
Morphosyntactic probing dataset

Languages

- UD: 122 languages
- mBERT: 104 languages
- XLM-RoBERTa: 100 languages
- intersection of these 3: 55 languages
- not enough morphosyntactic data: Chinese, Japanese, Vietnamese
- different tagging schema: Korean
- insufficient data in some languages
- external treebank for Albanian, silver data for Hungarian
- 42 languages

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Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Perturbations and Shapley values Shapley values

Morphosyntactic probing dataset Tags and POS

- UD has over 130 different morphosyntactic tags
- most are only used for one or a few languages
- we pick 4 common tags: case, gender, number, tense
- 4 open POS classes: adj, noun, propn, verb
- 14 combinations are available
 - (NOUN, Tense) and (PROPN, Tense) are linguistically implausible
 - $\langle ADJ, Tense \rangle$ only in Estonian
- most common tasks are (NOUN, Number) (37 languages), (NOUN, Gender) (32) and (VERB, Number) (27)

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

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Class number distribution



Most classes:

- \langle Hungarian, NOUN, Case \rangle : 18
- \langle Estonian, NOUN, Case \rangle : 15
- \langle Finnish, NOUN, Case \rangle : 12¹
- ▶ 〈Finnish, VERB, Case〉: 12

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Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

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Uralic languages

Perturbations and Shapley values Shapley values

¹Infrequent classes were omitted.

Probing tasks by language family



Number of morphological probing tasks by language family.

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Subword pooling Morphology in PLMs Ablations

Language-specific models

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Uralic language

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Probing dataset statistics

- 247 tasks
- 42 languages
- 10 language families (Indo-European subfamilies)
- 4 POS, 4 tags, 14 POS-tag combinations
- 2,000 train, 200 validaion and 200 test samples
- sentence length between 3 and 40 tokens, average 20.5

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Subword tokenization



- PLMs use subword tokenizers
- one token corresponds to multiple subwords, which one should we use?
- question for tagging problems too: POS and NER

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Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

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What do tokenizers do?

| | mBERT | | XLM-RoBERTa | | |
|----------|-------|------|-------------|------|--------|
| | count | 2+ | count | 2+ | _start |
| Arabic | 1.95 | 48.9 | 1.49 | 35.0 | 3.4 |
| Chinese | 1.58 | 53.5 | 2.13 | 88.5 | 86.6 |
| Czech | 2.04 | 53.0 | 1.7 | 45.2 | 1.6 |
| English | 1.25 | 14.3 | 1.25 | 16.9 | 0.8 |
| Finnish | 2.32 | 67.3 | 1.86 | 53.0 | 2.3 |
| French | 1.34 | 22.4 | 1.41 | 28.7 | 2.1 |
| German | 1.64 | 30.6 | 1.57 | 29.7 | 1.3 |
| Japanese | 1.6 | 43.0 | 2.25 | 94.6 | 92.9 |
| Korean | 2.44 | 75.7 | 2.16 | 67.3 | 9.0 |

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

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Perturbations and Shapley values Shapley values

Experimental setup

 9 typologically diverse languages .

- 3 tasks: morphosyntactic probing, POS, NER
- 9 subword pooling methods
- mBERT and XLM-RoBERTa
- feature extraction, no fine-tuning

| Method | Explanation |
|--------|--|
| FIRST | first subword unit |
| LAST | last subword unit |
| last2 | concatenation of the last two subword units |
| F+L | $wu_{\rm first} + (1-w)u_{\rm last}$ |
| SUM | elementwise sum |
| MAX | elementwise max |
| AVG | elementwise average |
| ATTN | Attention over the subwords, weights generated by an MLP |
| LSTM | biLSTM reads all vectors, final hidden state |

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languag

Perturbations and Shapley values Shapley values

Main results

- Morphology
 - ATTN is the best pooling strategy but its advantage over LAST is small and often not significant
 - FIRST is the worst

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Main results

- Morphology
 - ATTN is the best pooling strategy but its advantage over LAST is small and often not significant
 - FIRST is the worst
- POS and NER
 - depends on the language
 - we recommend trying a simple strategy (LAST) and a parametric one (ATTN or LSTM)



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Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs Ablations

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Conclusion

- most common: use first/last, max pooling
- the differences are very small
- last is usually better than first
- we pick either the first or the last based on the development data in all following experiments
 - last is better in over 90% of the tasks

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Subword pooling Morphology in PLMs

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Overview

- Do PLMs learn morphology?
- We use our 247 probing tasks
- We compare it against various baselines
- Extensive ablations

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Models and baselines

main focus: mBERT and XLM-RoBERTa other multilingual PLMs: XLM-Large, XLM-MLM-100, distilmBERT, mT5 main baseline: character LSTM (chLSTM) over full sentence, not pre-trained other baselines: subword LSTM on sentence, char LSTM and subword LSTM on target word only fastText: language-specific bag-of-ngrams word vectors Stanza: linguistic analysis toolkit for 70+ languages trained on UD

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Morphology in PLMs Ablations

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General results



Accuracy of the pre-trained and the baseline models grouped by POS.

- XLM-RoBERTa is slightly better than mBERT, larger models are even better
- chLSTM is the best baseline, it's closest in verbal tasks

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Neural pattern matching

Morphosyntactic probing of PLMs

Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Easiest and hardest languages



The best and the worst 5 languages by the average performance of mBERT and XLM-RoBERTa. The number of tasks in a particular language is listed in parentheses.

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Morphology in PLMs Ablations

Language-specific models

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Uralic language

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Model comparison

Which model is better² at how many tasks?



mBERT XLM-RoBERTa comparison by language family.

²Independent *t*-test over 10 runs.

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Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs

Morphology in PLMs Ablations

Language-specific models

Hungarian

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Ablations

Overview

- Probing has its fair share of criticism (Belinkov, 2021; Ravichander et al., 2021)
- We run various ablations to address them
- We find that:
 - 1. the choice of probe (linear, MLP, 2 layers) doesn't matter
 - 2. probing individual layers is no better or worse than probing the weighted sum of all layers
 - 3. fine-tuning is actually harmful (and wasteful)
 - 4. randomly initialized models (Voita and Titov, 2020) are much worse

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Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs

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Ablations

Pooling individual layers



The difference between probing a single layer and probing the weighted sum of layers. *concat* is the concatenation of all layers. 0 is the embedding layer.

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Ablations

Model ablations

mBERT-char: use character tokenization instead of subword tokenization

mBERT-emb: probe the embedding layer instead of the weighted sum of all layers



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs

Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values Shapley values

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values Shapley values

References

Language-specific models

Language-specific models Thesis 4

Monolingual PLMs are better in their respective languages than multilingual PLMs but the difference is small and often not statistically significant. Moreover both monolingual and multilingual PLMs can be successfully transfered to new languages as long as the new language uses the same writing system.

These contributions were published in (Ács et al., 2021b) and (Ács et al., 2021a).

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values Shapley values

Morphosyntactic evaluation tasks

| Morph tag | POS | #classes | Values |
|--------------|------|----------|---------------------|
| Case | noun | 18 | Abl, Acc,, Ter, Tra |
| Degree | adj | 3 | Cmp, Pos, Sup |
| Mood | verb | 4 | Cnd, Imp, Ind, Pot |
| Number[psor] | noun | 2 | Sing, Plur |
| Number | adj | 2 | Sing, Plur |
| Number | noun | 2 | Sing, Plur |
| Number | verb | 2 | Sing, Plur |
| Person[psor] | noun | 3 | 1, 2, 3 |
| Person | verb | 3 | 1, 2, 3 |
| Tense | verb | 2 | Pres, Past |
| VerbForm | verb | 2 | Inf, Fin |

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values Shapley values

Sequence tagging tasks

Part-of-speech tagging

- 1. Szeged UD Treebank (Farkas et al., 2012)
 - gold standard automatically converted to UD
 - 910/441/449 sentences
- 2. Webcorpus 2 subsample
 - tagged with emtsv (Indig et al., 2019)
 - 10,000/2,000/2,000 sentences

Named entity recognition

- 1. Szeged NER corpus
 - 8172/503/900 sentences

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Perturbations and Shapley values Shapley values

Experimental setup

- same probing architecture for morphology
- similar setup for POS and NER
- no fine-tuning due to resource limitations
- huBERT: the only Hungarian model at the time
- multilingual models: mBERT, XLM-RoBERTa, XLM-MLM-100, distilmBERT

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values Shapley values

Morphology results by Tranformer layer



The layerwise accuracy of morphological probes using the last subword. Shaded areas represent confidence intervals over 3 runs.

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values Shapley values

POS and NER results



Szeged POS

Szeged NER



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values Shapley values

Overview

Experimental setup:

- same as the Hungarian evaluation
- fine-tuning
- include every Uralic language with data regardless of model support

Models:

language-specific: HuBERT, FinBERT, EstBERT, Russian BERT multilingual: mBERT, XLM-RoBERTa random mBERT: random weights, mBERT tokenizer Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Languages and data

-

| Language | Code | Morph | POS | NER |
|---------------|-------|-------|------|------|
| Hungarian | [hu] | 26k | 2000 | 2000 |
| Finnish | [fi] | 38k | 2000 | 2000 |
| Estonian | [et] | 26k | 2000 | 2000 |
| Erzya | [myv] | 0 | 1680 | 1800 |
| Moksha | [mdf] | 0 | 164 | 400 |
| Karelian | [krl] | 0 | 224 | 0 |
| Livvi | [olo] | 0 | 122 | 0 |
| Komi Permyak | [koi] | 0 | 78 | 2000 |
| Komi Zyrian | [kpv] | 0 | 562 | 1700 |
| Northern Sami | [sme] | 0 | 2000 | 1200 |
| Skolt Sami | [sms] | 0 | 101 | 0 |

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

References

Size of training data for each language.

Morphology results



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

References

Pairs of bars: probing the first and last subword. Monolingual models are highlighted.

POS and NER results - Latin script



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encod<mark>er-decode</mark>r models for morphology

Neural pattern natching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

POS and NER results - Cyrillic script



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Conclusions

- monolingual models are the best when available
- multilingal models are close
- model transfer is surprisingly good even for unsupported languages
- state-of-the-art POS and NER models for minority languages with no language-specific effort

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values Shapley values

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungariar

Uralic language

Perturbations and Shapley values

Shapley value

References

Perturbations and Shapley values

Perturbations and Shapley values Thesis 5

The source of morphosyntactic information is often localized in a sentence. The systemic removal of certain information (perturbations) reveals where the information is stored. The role of context in morphosyntax can be quantified via Shapley values and the results often comply with linguistic intuitions.

These contributions were published in (Acs et al., 2023).

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languag

Perturbations and Shapley values

Shapley values

Perturbations

- Perturbations are a systematic removal of information from the sentence.
- We retrain the probe on the perturbed sentence and quantify the change as:

$$\mathsf{Effect}(m,t,p) = 1 - \frac{\mathsf{Acc}(m,t,p)}{\mathsf{Acc}(m,t)},$$

where m is the model, t is a probing task and p is a perturbation.

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley values

Perturbations

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- We retrain the probe on the perturbed sentence and quantify the change as:

$$\mathsf{Effect}(m,t,p) = 1 - \frac{\mathsf{Acc}(m,t,p)}{\mathsf{Acc}(m,t)},$$

where m is the model, t is a probing task and p is a perturbation.

| Perturbation | Explanation | Example |
|---------------------------|---|--|
| Original | | Then he ripped open Hermione 's letter and read it out loud . |
| TARG L ₂ | mask target word mask previous 2 words | Then he ripped open Hermione's letter and [M] it out loud. Then he ripped open Hermione's [M] [M] read it out loud. |
| R2 | mask next 2 words | Then he ripped open Hermione 's letter and read [M] [M] loud . |
| B ₂ PERMUTE | mask 2 on each side shuffle word order | Then he ripped open Hermione 's [M] [M] read [M] [M] loud . and open read Then letter . it out he ripped 's Hermione loud |

List of perturbation methods with examples. The target word is in **bold**. The mask symbol is abbreviated as [M].

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley values
Perturbed accuracy



Test accuracy of the perturbed probes grouped by POS. The first group is the average of all 247 tasks. The first two bars in each group are the unperturbed probes' accuracy.

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley value

Context masking results



case is the only tag affected strongly by context masking
L₂ is bigger than R₂, the left context is more important

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values

Shapley value

Context masking results



The effect of context masking on case tasks groupby by language family.

- std is larger than the effects
- L₂ is smaller than R₂ in Baltic and Indic languages
- context masking has neglible effect on Uralic languages

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values

Shapley values

Target masking and permutation

mBERT-targ 40 XLM-targ mBERT-permute 30 XLM-permute 20 effect 10 0 IE-Indic IE-Romance IE-Baltic IE-Germanic IE-Slavic IE-other Isolate Semitic Uralic

- TARG has by far the largest effect
- TARG and PERMUTE have opposite effects?

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values

Shapley value

Relationship between perturbations



TARG and PERMUTE indeed have a negative correlation
PERMUTE and B₂ are almost identical in effect

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values

Shapley value

Typology



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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language

Perturbations and Shapley values

Shapley values

References

Co-occurrence counts for each languages pair over 100 k-means clustering runs.

Shapley values

Formulation

Let's split the sentence into 9 parts or 9 players:

- T is the target word
- L_1 is the previous word, R_1 is the next word

and so on:

$$S = L_{4+}, L_3, L_2, L_1, T, R_1, R_2, R_3, R_{4+}$$

Each player's contribution can be quantified as:

$$\varphi(i) = \frac{1}{n} \sum_{S \subseteq N \setminus \{i\}} \frac{v(S \cup \{i\}) - v(S)}{\binom{n-1}{|S|}},$$

where the value function of a subset of players S is:

$$v(S) = 100 - 100 \cdot \frac{Acc_{S} - Acc_{all masked}}{Acc_{mBERT} - Acc_{all masked}}$$

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values

Shapley values

Shapley values Average Shapley values



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley values

Shapley values Values by POS



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values

Shapley values

Shapley values Values by tag



Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic languages

Perturbations and Shapley values

Shapley values

Shapley values Outliers



Least and most anomalous Shapley distributions. The first row are the mean Shapley values of the 247 tasks and the 5 tasks *closest* to the mean distribution, i.e. the least anomalous as measured by the dfm distance from the average Shapley values. The rest of the rows are the most anomalous Shapley values in descending order. For each particular task, its distance from the mean (dfm) is listed in parentheses above the graphs.

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley values

Shapley values Hindi and Urdu tasks



Shapley values in Indic tasks.

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley values

Shapley values



Shapley values in German tasks.

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian

Uralic language:

Perturbations and Shapley values

Shapley values

Number of experiments: appr. 500,000

- unperturbed and perturbed experiments run 10 times
- Shapley computation is exponential, 460,000 experiments
- 40 days of runtime
- Maximum 200 epochs. Early stopping in 98% of the time
- Average 22 epochs
- 43 tables, 63 figures, 117 references for now

Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values

Shapley values

References I

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Morphology in the Age of Pre-trained Language Models

Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languag

Perturbations and Shapley values Shapley values

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languas

Perturbations and Shapley values Shapley values

References III

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Judit Ács

Encoder-decoder models for morphology

Neural pattern natching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languag

Perturbations and Shapley values Shapley values

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic languag

Perturbations and Shapley values Shapley values

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Judit Ács

Encoder-decoder models for morphology

Neural pattern matching

Morphosyntactic probing of PLMs Subword pooling Morphology in PLMs Ablations

Language-specific models

Hungarian Uralic language

Perturbations and Shapley values Shapley values