# On Internal Merge <br> Steedman (2023) on CCGs and Minimalism 

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Hopf Algebra seminar

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## Introduction

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- This is taken as a core tenet of Steedman (2023): a derivation begins with inputs specifying exactly the combinatory potential to be used.
- The universal, type-dependent and language-independent rules are then applied to combine the inputs, which do not alter information.


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- Unite internal merge with external merge without adding discontinuity into the grammar, using as minimal expressive power as possible.
- Contrary to other proposals that eliminate movement (GPSG trace-feature passing, CG-nonstandard constituency, LFG lexicalization of locality, HPSG structural unification, etc.).
- These are too restrictive (grammar collapses to CFG) or too expressive (require additional constraints to then limit this).


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- Thus, internal merge (IM) is not different than external merge (EM).
- Expressive power of this system: "low near-context-free".
- Categories are defined functionally and semantically with functions and arguments, and IM discontinuities base-generated in the logical forms.


## Topics

- Components of CCG
- Lexical items
- Function application/composition
- Type raising
- External Merge
- Internal Merge
- Linguistic examples


## Defining CCGs and External Merge

## Components of CCG

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- The Categorial Assumption: Linguistic Categories are defined syntactically and semantically as functions and/or arguments.
(2) Contiguous merger universal rules
- The Adjacency Assumption: Rules are purely functional binary operations, limited to application, composition, and substitution, applying to strictly adjacent, phonologically-realized categories, which synchronously and monotonically compose logical forms (If) and concatenate phonological forms (pf).


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- $f$, a variables over logical forms corresponding to categories $\lambda y$.pres(walk y)


## (2) Merge: Function application

## Contiguous Merge I: Application Rules

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a. Forward application ( $>$ )
$X /{ }_{*} Y: f \quad Y: a \Rightarrow X: f a$
b. Backward application (<) $Y: a \quad X \backslash_{*} Y: f \Rightarrow X: f a$

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The Principle of Inheritance: Any category that appears in an input that also appears in the output of a rule must be feature-identical in both, including its slash-features, if any.
a. $Y: a \quad X / Y: f \nRightarrow X: f a$
b. $(X / Y) / W: f \quad Y: a \nRightarrow X / W: \lambda w . f w a$
c. $X_{i} / Y: f \quad Y: a \nRightarrow X_{j}: f a$

## Examples of Merge



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$$
\begin{aligned}
& 2 .
\end{aligned}
$$

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X / \Delta Y: f \quad Y / Z: g \Rightarrow X / Z: \lambda z . f(g z)
$$

b. Backward composition $(<B)$

$$
Y \backslash Z: g \quad X \backslash_{0} Y: f \Rightarrow X \backslash Z: \lambda z . f(g z)
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b. Backward composition $(<B)$
$Y \backslash Z: g \quad X \backslash_{\diamond} Y: f \Rightarrow X \backslash Z: \lambda z . f(g z)$
c. Forward crossing composition ( $>B_{\times}$)

$$
X / \times Y: f \quad Y \backslash Z: g \Rightarrow X \backslash Z: \lambda z . f(g z)
$$

d. Backward crossing composition ( $<\mathrm{B}_{\times}$)
$Y / Z: g \quad X \backslash_{\times} Y: f \Rightarrow X / Z: \lambda z . f(g z)$

## Merge: Function Composition (cont.)

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Function composition yields constituency effects:

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Function composition yields constituency effects:
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a. Forward level-2 composition ( $>\mathrm{B}^{2}$ )

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X /_{\diamond} Y: f(Y / Z)|W: g \Rightarrow(X / Z)| W: \lambda w \lambda z . f(g w z)
$$

b. Backward level-2 composition $\left(<B^{2}\right)$

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(Y \backslash Z)\left|W: g \quad X \backslash_{\bullet} Y: f \Rightarrow(X \backslash Z)\right| W: \lambda w \lambda z . f(g w z)
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$(Y \backslash Z)\left|W: g \quad X \backslash_{\diamond} Y: f \Rightarrow(X \backslash Z)\right| W: \lambda w \lambda z . f(g w z)$
c. Forward crossing level-2 composition ( $>\mathrm{B}_{\times}^{2}$ )
$X / \times Y: f \quad(Y \backslash Z)|W: g \Rightarrow(X \backslash Z)| W: \lambda w \lambda z . f(g w z)$
d. Backward crossing level-2 composition ( $<\mathrm{B}_{\times}^{2}$ ) $(Y / Z)\left|W: g \quad X \backslash_{\times} Y: f \Rightarrow(X / Z)\right| W: \lambda w \lambda z . f(g w z)$

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$$
X / Y: f(Y / Z) / W: g \nRightarrow(X / Z) \backslash W: \lambda w \lambda z . f(g w z)
$$

## Merge: Second-level Function Composition (cont.)

$\frac{\text { may }}{(\mathrm{S} \backslash \mathrm{NP}) / \mathrm{VP} \lambda p \lambda y \cdot m a y(p y)} \frac{\text { give }}{(\mathrm{VP} / \mathrm{PP}) / \mathrm{NP}: \lambda w \lambda x \lambda y \cdot(\text { give } x w y)}$<br>((S\NP)/PP)/NP : $\lambda w \lambda x \lambda y$.may (give xwy)

## Merge: Second-level Function Composition (cont.)

$\frac{\text { may }}{\frac{\text { give }}{(\mathrm{S} \backslash \mathrm{NP}) / \mathrm{VP} \lambda p \lambda y \cdot \operatorname{may}(p y)} \frac{(\mathrm{VP} / \mathrm{PP}) / \mathrm{NP}: \lambda w \lambda \times \lambda y \cdot(\text { give } \times w y)}{((\mathrm{S} \backslash \mathrm{NP}) / \mathrm{PP}) / \mathrm{NP}: \lambda w \lambda \times \lambda y \cdot \text { may }(\text { give } \times w y)}>\mathrm{B}^{2}}$

- Categories can grow completely unbounded, meaning CCG here is non-context-free.

The Combinatory Projection Principle (CPP): Combinatory rules apply to contiguous categories ("Adjacency"), must respect the linearization specified in the slash direction for the governing category ("Consistency"), and must project unchanged onto the resulting category any further categorial, selectional, and linearization information specified in either the governing or the dependent category ("Inheritance").

## Internal Merge

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2. Control: John tries to walk. John ${ }_{i}$ tries $P R O_{i}$ to walk.

## IM via raising and control

## Raising-to-subject

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| John | seems | to | walk. |
| :---: | :---: | :---: | :---: |
| $\overline{\mathrm{NP} \text { : john }} \overline{(\mathrm{S} \backslash \mathrm{NP}) / \mathrm{VP}_{\text {to }}: \lambda p \lambda y . \operatorname{pres}(\text { seem }(p y))}$ |  | $\overline{\mathrm{VP}_{\mathrm{to}} / \mathrm{VP}}$ : $\lambda$ | $\lambda y$. walk $(y)$ |
|  |  |  |  |
| S \NP : $\lambda y . \operatorname{pres(seem(walky))~}$ |  |  |  |
| S: pres(seem(walkjohn)) |  |  |  |

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|  |  | $\mathrm{VP}_{\text {to }}: \lambda y$. walk $(y)$ |
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|  | S:pres(seem(walk | kjohn)) |

## Subject-control

## IM via raising and control

## Raising-to-subject <br> seem: VP/VP to $: \lambda p \lambda y . \operatorname{seem}(p$ y)

$\frac{\text { John }}{\mathrm{NP}: \text { john }} \frac{\text { seems }}{(\mathrm{S} \backslash \mathrm{NP}) / \mathrm{VP}_{\text {to }}: \lambda p \lambda y \cdot p r e s(\operatorname{seem}(p y))} \frac{\text { to }}{\frac{\mathrm{VP} \text { to } / \mathrm{VP}: \lambda p \lambda y \cdot p y}{\mathrm{VP}_{\text {to }}: \lambda y \cdot \text { walk }(y)} \frac{\text { walk. }}{\mathrm{VP}: \lambda y \cdot \text { walk }(y)}}>$
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try: $V P_{+a} / V P_{t o}: \lambda p \lambda y . \operatorname{try}(p y) y$

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```
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$\frac{\mathrm{VP}_{\mathrm{to}}: \lambda y \cdot w a l k(y)}{\mathrm{S}_{+\mathrm{a}} \backslash \mathrm{NP}: \lambda y \cdot p r e s(t r y(\text { walky)y)}}$

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- For subject-control, the variable has two roles, one inside of the predicate $p$ and one outside of it, i.e. once as a subject controller and once as the controllee.
- Thus, the c-command relationship used for operator binding is here only established at If, which is why IM is effectively reduced to EM with additional If machinery.


## Type-raising

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$\frac{\frac{\text { Everything }}{\text { NP : everything }} \frac{\text { flows }}{\mathrm{S} \backslash \text { NP : } \lambda y \cdot \text { pres(flow } y)}}{\mathrm{S}: \text { pres (flow everything) }}<$

## Universal quantifiers and type-raising

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$$
\frac{\text { Everything }}{\frac{\text { NP }: \text { everything }}{S \backslash N P: \lambda y . p r e s(f l o w ~ y)}} \frac{\mathrm{S}: \text { pres }(\text { flow everything })}{<}
$$

$\frac{\frac{\text { Everything }}{\mathrm{S} /(\mathrm{S} \backslash \mathrm{NP}): \lambda p \forall y[\text { thing } y \Rightarrow p y]} \frac{\text { flows }}{\mathrm{S} \backslash \mathrm{NP}: \lambda y \cdot p r e s(\text { flow } y)}}{\mathrm{S}: \forall y[\text { thing } y \Rightarrow \operatorname{pres}(\text { flow } y)]}$

## Type-raising

- This then results in having to allow all NPs and transitive verbs to "type raise", e.g. objects to take scope over matrix domain.


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| Someone | sees everything |
| :---: | :---: |
| $\begin{gathered} \mathrm{S} /(\mathrm{S} \backslash \mathrm{NP}) \\ : \lambda p . p(\text { some person }) \end{gathered}$ | $(\mathrm{S} \backslash \mathrm{NP}) / \mathrm{NP}$ |
|  | $: \lambda x \lambda y . \operatorname{pres}($ see $x y): \lambda p \lambda y . \forall x[$ thing $x \Rightarrow p \times y]$ |
|  | $\mathrm{S} \backslash \mathrm{NP}: \lambda y . \forall x[$ thing $x \Rightarrow \operatorname{pres}($ see $x y)]$ |
|  | $x[p r e s($ see $x($ some person) $)$ ] |

## Type-raising (cont.)

Type-raised generalized quantifier is the only way for universal quantifiers to take wide-scope without quantifier-raising.

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| A | girl | held | every | chipmunk. |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \overline{\left(\mathrm{S} /\left(\mathrm{S} \backslash \mathrm{NP}_{3 \mathrm{~s}}\right)\right) / \mathrm{N}_{3 \mathrm{~s}}} \\ : \lambda n \lambda p . p(a n) \end{gathered}$ | $\begin{aligned} & \mathrm{N}_{3 \mathrm{~s}} \\ & : \text { girl } \end{aligned}$ | $\begin{aligned} & \left(\mathrm{S} \backslash \mathrm{NP}_{\mathrm{agr}}\right) / \mathrm{NP} \\ & : \lambda x \lambda y \cdot \text { past } \text { hold } x y) \end{aligned}$ | $\begin{gathered} \left(\left(\mathrm{S} \backslash \mathrm{NP} \mathrm{P}_{\text {agr }}\right) \backslash\left(\left(\mathrm{S} \backslash \mathrm{NP}_{\mathrm{agr}}\right) / \mathrm{NP}\right)\right) / \mathrm{N}_{3 \mathrm{~s}} \\ : \lambda n \lambda p \lambda y . \forall x[n \times \rightarrow p \times y] \end{gathered}$ | $\mathrm{N}_{3 \mathrm{~s}}$ : chipmunk |
| $\overline{\mathrm{S} /\left(\mathrm{S} \backslash \mathrm{NP}_{3 \mathrm{~s}}\right): \lambda p . p(a \mathrm{gir}}$ ) |  | $\begin{gathered} \left(\mathrm{S} \backslash N \mathrm{NP}_{\mathrm{agr}}\right) \backslash\left(\left(\mathrm{S} \backslash \mathrm{NP}_{\mathrm{agr}}\right) / \mathrm{NP}\right) \\ : \lambda p \lambda y \cdot \forall x[\text { chipmunk } x \rightarrow p \times y)] \end{gathered}$ |  |  |
|  |  | $\mathrm{S} \backslash$ NP $\mathrm{agr}: \lambda y . \forall x[$ chipmunk $x \rightarrow$ past(hold $x y$ )] |  |  |
|  |  | $\forall x[$ chipmunk $x \rightarrow$ | st(hold $\times($ a girl) $)$ ] |  |

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- someone: $N P^{\uparrow}: \lambda p \lambda \hat{y} . p($ some person) $\hat{y}$
- an: $N P^{\uparrow} / N: \lambda n \lambda p \lambda \hat{y} . p(a n) \hat{y}$
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- Type-raising allows for scrambling word orders.
- Caveat: not a free combinatory rule to be used for syntactic derivations, only available as a morpho-lexical schema.


# Type-Raising: Scrambling in Germanic 

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| *Sara | gave | cake | her sister. |
| :---: | :---: | :---: | :---: |
| $\overline{\mathrm{S} / \diamond_{*}(\mathrm{~S} \backslash \mathrm{NP})}$ | $\overline{((\mathrm{S} \backslash \mathrm{NP}) / \mathrm{NP}) / \mathrm{NP}}$ | $\overline{(\mathrm{S} \backslash \mathrm{NP}) \backslash \diamond_{*}((\mathrm{~S} \backslash N \mathrm{NP}) / \mathrm{NP})} \underset{*<\mathrm{B}_{\times}}{ }$ | $\overline{(\mathrm{S} \backslash \mathrm{NP}) \backslash \diamond *((\mathrm{~S} \backslash \mathrm{NP}) / \mathrm{NP})}$ |

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$\frac{* \text { Sara }}{\mathrm{S} / \diamond_{*}(\mathrm{~S} \backslash \mathrm{NP})} \frac{\text { gave }}{\frac{\text { cake }}{((\mathrm{S} \backslash \mathrm{NP}) / \mathrm{NP}) / \mathrm{NP}} \frac{\mathrm{S}(\mathrm{S} \backslash \mathrm{NP}) \backslash \diamond_{*}((\mathrm{~S} \backslash \mathrm{NP}) / \mathrm{NP})}{*<\mathrm{B}_{\times}}} \frac{\text { her sister. }}{* * *} \frac{\mathrm{~S} \backslash \mathrm{NP}) \backslash \diamond_{*}((\mathrm{~S} \backslash \mathrm{NP}) / \mathrm{NP})}{}$
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## German scrambling

Type-raising of arguments (morpho-lexical and order-preserving) can interact with function composition to derive scrambling effects in languages with freer word-order.
(1) Johann hat [auf dem Markt] [die Lebensmittel gekauft]. Johann has at the market the groceries bought. 'Johann bought the groceries at the market.'
(2) Johann hat [die Lebensmittel] [auf dem Markt] gekauft. Johann has the groceries at the market bought.
'Johann bought the groceries at the market.'
(3) *Johann [die Lebensmittel] hat [auf dem Markt] gekauft. Johann the groceries has at the market bought.
'Johann bought the groceries at the market.'

## CCG and German scrambling



## CCG and German scrambling (cont.)

| *Johann Johann | die Lebensmittel the groceries | hat has | auf dem Markt at the market | gekauft. <br> bought. |
| :---: | :---: | :---: | :---: | :---: |
| S/(S\NP) | $\mathrm{VP} /\left(\mathrm{VP} \backslash \mathrm{NP}_{\text {acc }}\right)$ | $\left.\overline{(S m a i n ~} \backslash N P_{\text {nom }}\right) / V P$ | VP/VP | $\overline{\mathrm{V} \backslash \text { \P }{ }_{\text {acc }}}$ |
|  |  |  | VP $\backslash$ NP |  |
|  |  | ( $\mathrm{S}_{\text {main }}$ | $\left.\mathrm{SP}_{\text {nom }}\right) \backslash N \mathrm{P}_{\text {acc }}$ |  |

*     *         * 


# IM: Wh-Movement 

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Topicalization:

## Wh-movement

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Topicalization:
$\frac{\text { Books, }}{\frac{\text { she }}{\mathrm{S}_{\mathrm{t}} /(\mathrm{S} / \mathrm{NP}): \lambda p . p \text { books }} \frac{\text { hates. }}{\frac{\mathrm{S} /\left(\mathrm{S} \backslash \mathrm{NP}_{3 \mathrm{~s}}\right): \lambda p . p \text { her }}{} \frac{\mathrm{S} / \mathrm{NP}: \lambda x \cdot p r e s(\text { hate } \times \text { her })}{\left(\mathrm{S}_{3 \mathrm{~s}}\right) / \mathrm{NP}: \lambda x \lambda y \cdot p r e s(\text { hate } \times y)}}>\mathrm{B}} \mathrm{S}_{\mathrm{t}}:$ pres(hate books her) $\gg$

## Wh-question formation

- Auxiliaries (in English) specify the subject-inversion, not the subject.


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| What | does | she | hate? |
| :---: | :---: | :---: | :---: |
| $\overline{\mathrm{S}_{\mathrm{whq}} /\left(\mathrm{S}_{\mathrm{inv}} / \mathrm{NP}\right)}$ <br> : $\lambda p \lambda w h . p$ wh | $\left(\mathrm{S}_{\text {inv }} / \mathrm{VP}\right) / \mathrm{NP}_{3 \mathrm{~s}}$ | $\overline{\left(\mathrm{S}_{\text {inv }} / \mathrm{VP}\right) \backslash\left(\left(\mathrm{S}_{\text {inv }} / \mathrm{VP}\right) / \mathrm{NP}_{3 \mathrm{~s}}\right)}$ | $\begin{gathered} \mathrm{VP} / \mathrm{NP} \\ : \lambda x \lambda y . \text { hate } x y \end{gathered}$ |
|  | : $\lambda \mathrm{y} \lambda \mathrm{p} . \mathrm{pres}(\mathrm{p} y)$ | : $\lambda$ p.p her |  |
|  | $\mathrm{Sinv}_{\text {in }} / \mathrm{V}$ | : $\lambda$ p.pres(p her) |  |
|  |  | Sinv/NP: $\lambda \times$.pres(hate $\times$ her) |  |
|  | $\mathrm{S}_{\text {whq }}: \lambda$ | wh.pres(hate wh her) |  |

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| $\overline{S_{\text {whq }} /\left(S_{\text {inv }} / N P\right)}$ <br> : $\lambda p \lambda w h . p$ wh | $\begin{aligned} & \left(\mathrm{S}_{\mathrm{inv}} / \mathrm{VP}\right) / \mathrm{NP}_{3 \mathrm{~s}} \\ & \lambda y \lambda p . \operatorname{pres}(\mathrm{p} y) \end{aligned}$ | $\begin{gathered} \overline{\left(\mathrm{S}_{\text {inv }} / \mathrm{VP}\right) \backslash\left(\left(\mathrm{S}_{\text {inv }} / \mathrm{VP}\right) / \mathrm{NP}_{3 \mathrm{~s}}\right)} \\ : \\ \\ \lambda p . p \mathrm{her} \end{gathered}$ | $\begin{gathered} \mathrm{VP} / \mathrm{NP} \\ \lambda x \lambda y \text { hate } x y \end{gathered}$ |
|  | $\mathrm{S}_{\text {inv }} / \mathrm{V}$ | $\lambda p . \operatorname{pres}(p$ her) |  |
|  |  | inv/NP: $\lambda \times$.pres(hate $\times$ her) |  |
|  | $S_{\text {whq }}: \lambda w$ | h.pres(hate wh her) |  |

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|  | : $\lambda y \lambda$ p.pres( $p y$ ) | $\lambda p . p$ her |  |
|  | $\mathrm{S}_{\text {inv }}$ | $\lambda p . \operatorname{pres}(p$ her) |  |
|  |  | $S_{\text {inv/ } / \mathrm{NP}: ~ \lambda x . p r e s(h a t e ~}^{\text {x her) }}$ |  |
|  | $\mathrm{S}_{\mathrm{whq}}: \lambda$ | wh.pres(hate wh her) |  |

- Wh-item has copies of what it has moved out of, $p$, and $\lambda$-binder.
- Its syntactic category is specified as at the left edge of the sentence.
- Its argument is thus passed into the wh-item as $p$.


## Conclusion

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- IM is thus reduced at the level of syntactic derivation to EM, which reduces Move to purely local contiguous Merge. This is in comparison to Minimalist systems which are not entirely synchronous, as opposed to CCG here.
- Probes, goals, valuations, feature deletion, and visibility conditions can all be eliminated.


## References

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